

Hi, I need all of the following answered correctly and all working shown. There are a total of 15 questions including A and B's etc. There are 2 graph questions, which I'll also need a copy of the graph, but hopefully that's not too hard. This test is based of NZ's High school NCEA level 3. I don't mind where you put the working and answers, but if you use this page please just put the working and answers in Blue or something. Thanks =)

$\Theta$  = Theta

$$\frac{dy}{dx}$$

1) Find  $\frac{dy}{dx}$  for each of the following. You do not need to simplify your answers.

a)  $y = \log_e 3x + 8x^3$

b)  $y = \sqrt[3]{2x-1}$  (The square root sign is meant to be over the entire  $2x-1$ )

c)  $y = e^x \operatorname{cosec} x$

d)  $\frac{e^{4x+3}}{4x+3}$

2) If  $g(x) = 7x^3 - 2x^2 + 4x - 8$  find the third derivative  $g'''(x)$

$$\frac{dy}{dx}$$

3) If  $x = \sin \theta$  and  $y = \sec \theta$ , find  $\frac{dy}{dx}$  in terms of  $\sin \theta$  and  $\cos \theta$

4) A curve is defined by the parametric equations  $x=t^2$  and  $y = 2t+1$   
Find the equation of the tangent at the point where  $t = 2$

5) The height in metres of a bullet fired up into the air after  $t$  seconds is given by  
 $h = 2000t - 200t^2$

Find the maximum height the bullet reaches. (A test to check you have found the maximum height is expected.)

6) Nico's bubble blowing machine blows spherical bubbles whose surface area,  $S$ , increases at the rate of  $25\text{cm}^2/\text{s}$ .  
What is the rate of increase of the radius,  $r$ , of the bubble when the radius is  $5\text{cm}$ ?

7)  $f(x) = x^3 - 3x + 2$

- a) Find the coordinates of any local minimum point, maximum point or point of inflection. Make sure you apply and appropriate test for each.
- b) Use the factor theorem to help you find the intercepts with the axes.
- c) Sketch the graph of  $f(x)$  showing the above features.
- d) Give the values of  $x$  for which the graph is concave down.

8) A pile of sand is a roughly conical pile. The slant edge of the pile is  $6.0\text{m}$ .

- a) What is the height of the pile when the Volume of sand in it is at its maximum
- b) A truck operator contracted to shift the sand wants to know how many cubic metres there are. What answer should he be given? Justify your answer with a reference to the situation described