

Hi, I need all of the following answered correctly and all working shown. There are a total of 15 questions including A and B's etc. There are 2 graph questions, which I'll also need a copy of the graph, but hopefully that's not too hard. This test is based of NZ's High school NCEA level 3. I don't mind where you put the working and answers, but if you use this page please just put the working and answers in Blue or something. Thanks =)

Θ = Theta

$$\frac{dy}{dx}$$

1) Find $\frac{dy}{dx}$ for each of the following. You do not need to simplify your answers.

a) $y = \log_e 3x + 8x^3$

b) $y = \sqrt[3]{2x-1}$ (The square root sign is meant to be over the entire $2x-1$)

c) $y = e^x \operatorname{cosec} x$

d) $\frac{e^{4x+3}}{4x+3}$

2) If $g(x) = 7x^3 - 2x^2 + 4x - 8$ find the third derivative $g'''(x)$

$$\frac{dy}{dx}$$

3) If $x = \sin \theta$ and $y = \sec \theta$, find $\frac{dy}{dx}$ in terms of $\sin \theta$ and $\cos \theta$

4) A curve is defined by the parametric equations $x=t^2$ and $y = 2t+1$
Find the equation of the tangent at the point where $t = 2$

5) The height in metres of a bullet fired up into the after t seconds is given by
 $h = 2000t - 200t^2$

Find the maximum height the bullet reaches. (A test to check you have found the maximum height is expected.)

6) Nico's bubble blowing machine blows spherical bubbles whose surface area, S , increases at the rate of $25\text{cm}^2/\text{s}$.
What is the rate of increase of the radius, r , of the bubble when the radius is 5cm ?

7) $f(x) = x^3 - 3x + 2$

- a) Find the coordinates of any local minimum point, maximum point or point of inflection. Make sure you apply and appropriate test for each.
- b) Use the factor theorem to help you find the intercepts with the axes.
- c) Sketch the graph of $f(x)$ showing the above features.
- d) Give the values of x for which the graph is concave down.

8) A pile of sand is a roughly conical pile. The slant edge of the pile is 6.0m .

- a) What is the height of the pile when the Volume of sand in it is at its maximum
- b) A truck operator contracted to shift the sand wants to know how many cubic metres there are. What answer should he be given? Justify your answer with a reference to the situation described